



University Of Jordan - Aqaba
Faculty of Systems and information technology
Department of computer information systems

Calculus 2
Date : 18/11/2015

Midterm Exam
2015/2016

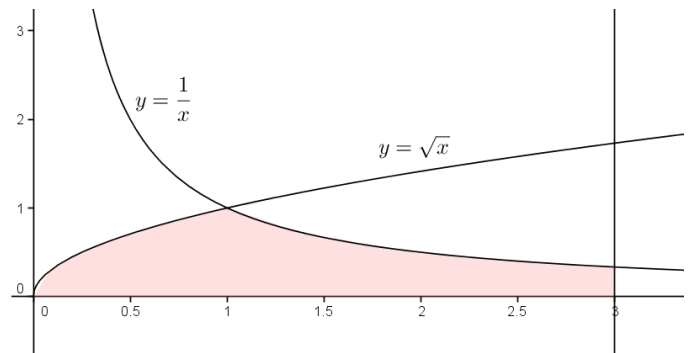
1st Semester

Student name:
Student number:

Question 1. Find the area of region enclosed between the curves

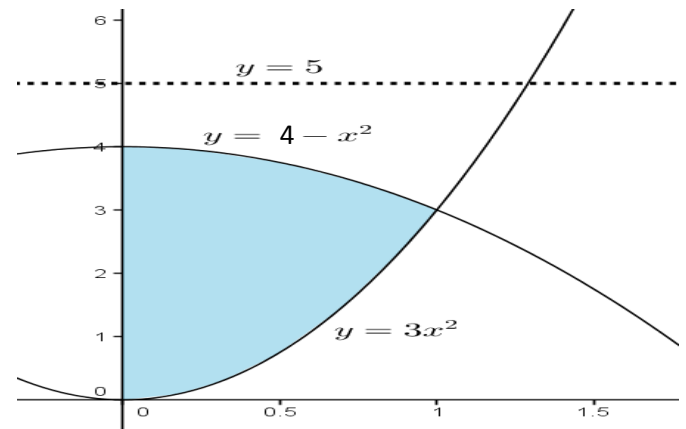
$$f(x) = \frac{1}{x}, \quad g(x) = \sqrt{x}, \quad y = 0 \quad \text{and} \quad x = 3.$$

$$\begin{aligned} A &= \int_0^1 x^{\frac{1}{2}} \cdot dx + \int_1^3 \frac{1}{x} \cdot dx \\ &= \left[\frac{2}{3} \cdot x^{\frac{3}{2}} \right]_0^1 + [Ln(x)]_1^3 = \frac{2}{3} + Ln(3) \end{aligned}$$



Question 2. Find the volume of the solid that results when the region enclosed by $y = 3x^2$, $y = 4 - x^2$ and $x = 0$ is revolved about the line $y = 5$.

$$\begin{aligned} A &= \pi \int_0^1 (5 - 3x^2)^2 \cdot dx - \int_0^1 (5 - 4 + x^2)^2 \cdot dx \\ &= \pi \int_0^1 25 - 30x^2 + 9x^4 \cdot dx - \pi \int_0^1 1 + 2x^2 + x^4 \cdot dx \\ &= \pi \left[25x - \frac{30x^3}{3} + \frac{9x^5}{5} \right]_0^1 - \left[x + \frac{2x^3}{3} + \frac{x^5}{5} \right]_0^1 \\ &= \pi \left[25 - 10 + \frac{9}{5} \right] - \pi \left[1 + \frac{2}{3} + \frac{1}{5} \right] = \frac{84}{5} \pi - \frac{28}{15} \pi = \end{aligned}$$



Question 3. Find

1. $\int \frac{t \cdot e^t}{(t+1)^2} \cdot dt$

$$\left\{ \left\langle \begin{aligned} y = t+1 &\Rightarrow dy = dt \\ \int \frac{(y-1)e^{y-1}}{y^2} \cdot dy &= \int \frac{y}{y^2} \cdot e^{y-1} \cdot dy - \int \frac{1}{y^2} \cdot e^{y-1} \cdot dy \\ &= \int \frac{1}{y} \cdot e^{y-1} \cdot dy - \int \frac{1}{y^2} \cdot e^{y-1} \cdot dy \\ \left\langle \begin{aligned} u &= \frac{1}{y} & dv &= e^{y-1} \cdot dy \\ du &= \frac{-1}{y^2} \cdot dy & v &= e^{y-1} \end{aligned} \right\rangle \\ &= \frac{1}{y} \cdot e^{y-1} - \int \frac{-1}{y^2} \cdot e^{y-1} \cdot dy - \int \frac{1}{y^2} \cdot e^{y-1} \cdot dy \\ &= \frac{1}{y} \cdot e^{y-1} + c \end{aligned} \right\rangle \right\}$$

2. $\int \frac{x+1}{2x-x^2} \cdot dx$

$$\left\{ \left\langle \begin{aligned} \frac{x+1}{x \cdot (2-x)} &= \frac{A}{x} + \frac{B}{2-x} \\ x+1 &= A(2-x) + Bx \\ \begin{aligned} x=0 &\Rightarrow 1 = 2A \Rightarrow A = \frac{1}{2} \\ x=2 &\Rightarrow 3 = 2B \rightarrow B = \frac{3}{2} \end{aligned} \\ \int \frac{1}{x} + \frac{3}{2-x} \cdot dx &= \frac{1}{2} \ln|x| + \frac{3}{2} \ln|2-x| + c \end{aligned} \right\rangle \right\}$$

3. $\int \sec^4 x \cdot \tan^9 x \cdot dx$

$$\left\{ \left\langle \begin{aligned} \int \tan^9 x \sec^2 x \cdot \sec^2 x \cdot dx &= \int \tan^9 x \cdot (1 + \tan^2 x) \cdot \sec^2 x \cdot dx \\ u = \tan x &\Rightarrow du = \sec^2 x \cdot dx \\ \int u^9 \cdot (1 + u^2) \cdot \sec^2 x \cdot \frac{du}{\sec^2 x} &= \int u^9 + u^{11} \cdot du = \frac{u^{10}}{10} + \frac{u^{12}}{12} + c \end{aligned} \right\rangle \right\}$$

4. $\int \sqrt{x} \cdot \sin(\sqrt{x}) \cdot dx$

$$\left\{ \left\langle \begin{aligned} u &= \sqrt{x} \\ du &= \frac{1}{2\sqrt{x}} \cdot dx \\ \int u \cdot \sin u \cdot 2u \cdot du &= \int 2u^2 \cdot \sin u \cdot du \\ &= 2u^2 \cdot \cos u - 4u \cdot \sin u - 4 \cos u + c \end{aligned} \right\rangle \right\}$$

u	dv
$2u^2$	$\sin u$
$4u$	$\cos u$
4	$-\sin u$
0	$-\cos u$